

General Problem Solving Guide

List given information, define variables, sketch picture:

Name:

KEY

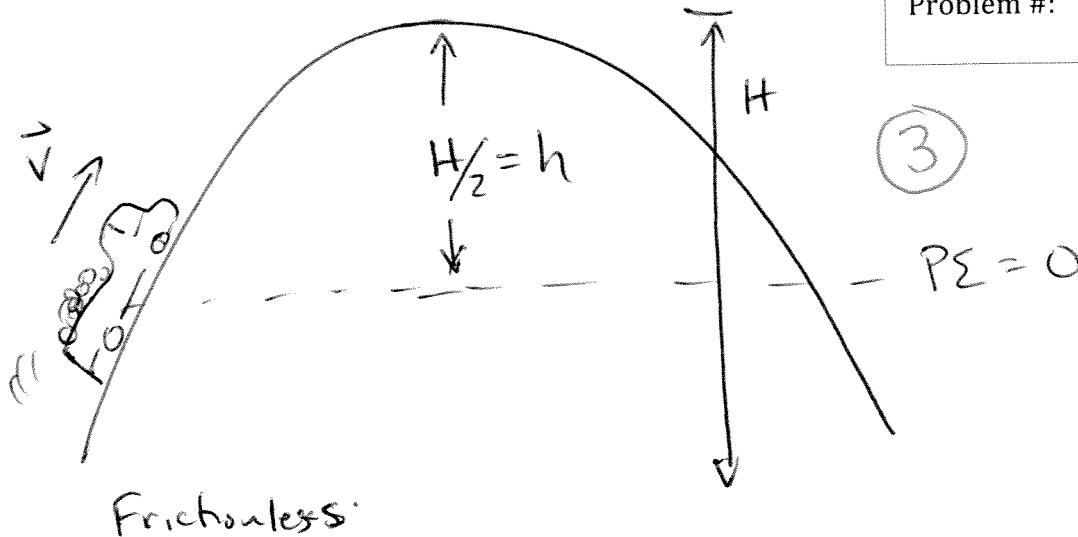
Lab Time:

Date:

Test Code:

Total
10

Problem #:



Simplify question, list target quantity:

⑤ Is truck going fast enough?
(have enough energy to get over hill)

List all related quantitative relationships:

② $E_i = E_f$

$$KE = \frac{1}{2}mv^2$$

$$PE = mgh$$

$$E = KE + PE$$

Outline approach, sketch diagrams if needed (or sketch next to pictures above):

⑤.5 Set initial and final energies equal.
Compare velocity needed to truck's velocity
Check if mass makes a difference

Obtain a general solution:

Check Units: _____

$$mgh_i + \frac{1}{2}mv_i^2 = mgh_f + \frac{1}{2}mv_f^2 \quad (1)$$

$$\frac{m}{s} = \left(\frac{m}{s^2} m\right)^{1/2} = \left(\frac{m^2}{s^2}\right)^{1/2} = m/s$$

mass cancels

$$h_i = 0 \text{ m}$$

$$h_f = h$$

$$v_i = v$$

$$v_f = 0 \text{ m/s} \quad (\text{truck barely makes it to the top of the hill})$$

Check Limiting Cases: _____

$$h \uparrow \quad v \uparrow \quad \checkmark$$

$$g \uparrow \quad v \uparrow \quad \checkmark$$

$$\text{mass} \uparrow \quad \text{doesn't matter} \quad \checkmark$$

$$\frac{1}{2}v^2 = gh$$

$$v^2 = 2gh$$

$$v = \sqrt{2gh}$$

Note $h = H/2$

$$A: H = 20 \text{ m} \quad v_0 = 13.5 \text{ m/s}$$

$$v = \sqrt{2 \cdot 9.8 \frac{\text{m}}{\text{s}^2} \cdot 10 \text{ m}}$$

$$v = 14 \text{ m/s}$$

$$B: H = 24 \text{ m} \quad v_0 = 16 \text{ m/s}$$

$$v = 15.3 \text{ m/s}$$

$$C: H = 30 \text{ m} \quad v_0 = 18 \text{ m/s}$$

Obtain a numeric solution: _____

(i.e. plug in the numbers)

$$A: 13.5 \text{ m/s} < 14 \text{ m/s} \quad \text{DUPS!}$$

$$B: 16 \text{ m/s} > 15.3 \text{ m/s} \quad \text{SUCCESS}$$

$$C: 18 \text{ m/s} > 17.2 \text{ m/s} \quad \text{SUCCESS}$$

* TRUCK DOES NOT MAKE IT OVER!

Why is solution reasonable? Explain.

Units check

Limiting cases check

Velocity seems reasonable

Energy conservation is a good choice for this problem

Shape of hill doesn't matter

Mass doesn't matter (just velocity)

$$v = 17.2 \text{ m/s}$$